## 1 Subword complexes, Brick polytopes and brick polyhedra

There are powerful techniques to describe the Tamari lattice and the associahedron in terms of subword complexes and brick polytopes in the context of Coxeter groups, which in turn are also related to cluster complexes and generalized associahedra arising in the theory of cluster algebras. This project concerns learning about these topics [1, 3, 4, 2].

## References

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